recombination.prob Probability of recombination out of identical-by-descent

Usage

recombination.prob(centimorgan, num.meioses, chance.decent)

Arguments

centimorgan vector of distances in centiMorgans

num.meioses number of meioses that can happen between two candidate identical-by-descent segments (e.g. 1 for parent-child, 2 for siblings, 4 for 1st cousins, etc...

chance.descent

chance that two chromosomes from two relatives are identical-by-descent at a nucleotide position (SNP)

Math

Let d denote the distance between nucleotides in Morgans.

Let m denote number of meioses.

Let $\alpha = \Pr(I_i)$ denote probability of nucleotides being identical-by-descent (unconditional IBD SNP probability).

Let q denote the multi-meiosis recombination function.

$$q(d, m, \alpha) = (1 - \alpha) \left(1 - e^{-d \cdot m/(1 - \alpha)}\right)$$

Note appropriate properties:

$$q(0, m, \alpha) = 0$$

$$q(\infty, m, \alpha) = 1 - \alpha$$

$$\frac{dq}{dd}(0,m,\alpha) = m$$